

N.B. 1. Question No. 1 is compulsory.

2. Attempt any **Four** out of remaining.

3. Assume suitable data if **necessary** and **justify** the assumptions.

4. Figures to the **right** indicate full marks.

Algorithms & Complexity

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Q1.A. Write a function for Bubble sort and show computation of its space and time complexity. [10]

B. Give a dynamic-programming solution to the 0-1 Knapsack Problem that runs in  $O(nW)$  Times, where  $n$  is the number of items and  $W$  is the maximum weight of items that the thief can put in his knapsack. [10]

Q2.A. Prove that Clique is NP-Complete. [10]

B. Compute Longest common subsequence for  $A = 0001101100$  and  $B = 1110010010$ . [10]

Q3.A. Find a feasible solution or determine that no feasible solution exists for the following systems of difference constraints. Write the algorithm for the same and give its complexity. [10]

$$x_1 - x_2 \leq 4$$

$$x_1 - x_5 \leq 5$$

$$x_2 - x_4 \leq -6$$

$$x_3 - x_2 \leq 4$$

$$x_4 - x_1 \leq 3$$

$$x_4 - x_3 \leq 5$$

$$x_4 - x_5 \leq -3$$

$$x_5 - x_3 \leq -4$$

$$x_5 - x_4 \leq -8$$

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B. Discuss the Bitonic Sorting Technique. [10]

Q4.A. Insert the following keys 5, 6, 9, -3, 28, 89, 50, 32, 96, 0 in a hash table of length  $m=13$  using open addressing with primary hash function  $h(k) = k \bmod m$ . show results inserting keys using [10]

i. Linear probing

ii. Quadratic probing with  $C_1 = 1$  and  $C_2 = 3$ .

B. Give RSA encryption algorithm. [10]

Consider a RSA key set with  $p=29$ ,  $q=11$ ,  $n = 319$  and  $e=3$ .

What value of 'd' should be stored in secret key ?

What is the encryption of the message  $M = 100$  ?

Q5.A. Find an optimal parenthesization of a matrix-chain product whose sequence of dimensions is  $\langle 5 \ 10 \ 3 \ 5 \ 15 \ 30 \ 6 \rangle$ . [10]

B. Given Below is the weight matrix  $W$  for the graph consisting of five nodes  $\{S, B, C, D, E\}$ . Find the shortest path from node  $S$  to all other nodes. [10]

Weight matrix  $W =$

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	S	B	C	D	E
S	0	10	$\infty$	$\infty$	5
B	$\infty$	0	1	$\infty$	2
C	$\infty$	$\infty$	0	-4	$\infty$
D	7	$\infty$	6	0	$\infty$
E	$\infty$	-3	9	2	0

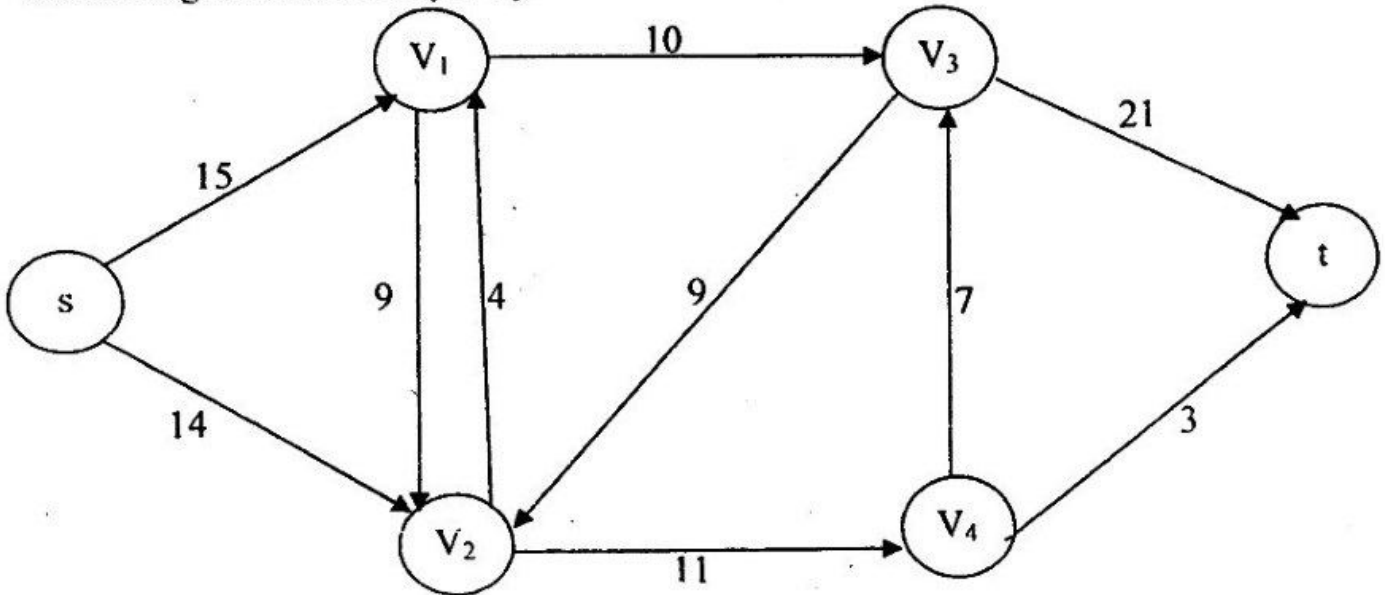
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Q6.A. Find the maximum flow for the network given below.  
Give the algorithm and complexity

[20]



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Q7. Write a short note on any **four** of the following.

[20]

- Discuss the various models of computation.
- B<sup>+</sup> Tree with operations insertion and deletion
- Versions of Problems.
- Master method for recurrences
- RB Tree with operation insertion
- Chinese Remainder Theorem.

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