

INS 1

SEMI/Control Syst. Design

28/05/2015

QP Code : 3340

(3 Hours)

[Total Marks : 80

- N. B. : (1) Question No. 1 is **compulsory**.
 (2) Solve any **three** questions from remaining **five** questions.
 (3) Assume suitable data if needed.

1. Attempt the following :— 20

(a) State the advantages of modern control theory over conventional theory.

(b) Obtain the transfer function of the system.

$$\dot{x}_1 = -2x_1 - x_2 + u$$

$$\dot{x}_2 = -3x_1 - x_2 + u$$

$$y = x_1$$

(c) Compare lead / lag / lag-lead compensator. Also draw poles & zeros plot of all.

(d) What is Caley Hamilton theorem? Explain the steps to solve for STM using the Caley Hamilton theorem.

2. (a) Derive the transfer function of lag-lead compensator. 10

(b) Obtain diagonalized matrix (M) for given system matrix :

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -3 & -3 \end{bmatrix}$$

3. (a) For the unity feedback control system with PID controller is used to control the system. The plant transfer function is 10

$$G(s) = \frac{K}{s(s+1)(s+5)}$$

Determine PID controller.

(b) An open loop control system with : 10

$$G(s) = \frac{K}{s^2}$$

The system is compensated to meet the following specifications using lag compensator

$$K_v = 5/\text{sec}$$

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JP-Con. : 11314-15.

4. (a) Determine the state transition matrix for the system : 10

$$A = \begin{bmatrix} -2 & 1 \\ -2 & -3 \end{bmatrix} \text{ also find the response if the initial condition is}$$

$$x(0) = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

- (b) Explain the design steps of lag compensator using Bode plot 10

5. (a) Design an observer for the plant 10

$$G(s) = \frac{10(s+2)}{s(s+4)}$$

Desired observer poles are at $-5, -5$

- (b) Check the following systems are completely controllable & observable: 10

$$(i) \dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

$$y = [1 \quad 0] x$$

$$(ii) \dot{x} = \begin{bmatrix} -2 & 1 \\ 1 & -2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$$

$$y = [1 \quad -1] x$$

6. (a) Consider a plant transfer function 10

$$G(s) = \frac{10}{(s+1)(s+5)}$$

Design state feedback gain matrix to meet the following specifications:

$$\xi = 0.5$$

$$\omega_n = 5 \text{ rad/sec}$$

- (b) For a unity feedback system 10

$$G(s) = \frac{K}{s(s+1)}$$

Design a suitable compensator with the following specifications :-

$$K_v = 12/\text{sec}$$

$$\text{Phase margin} = 40^\circ$$